

# Interference Alignment for High Rate Transmission in Partially Connected Multi-User Two-Way Relay Networks



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Motivation / Objectives

Interference alignment (IA) in two-way relaying networks

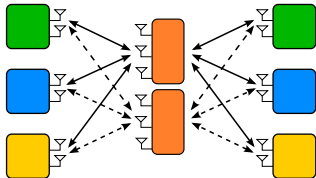
Introduction of a partially connected network

Proposed algorithm

Simulation results

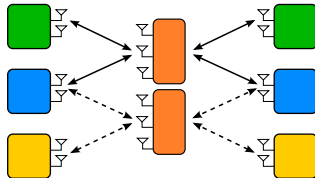
Summary

- ▶ Bidirectional communication via intermediate half-duplex relays
- ▶ Direct links between the nodes not utilized



## Full connected network

- ▶ All relays are connected to all nodes
- ▶ All relays can help to perform IA in the whole network
- ▶ Requires global CSI

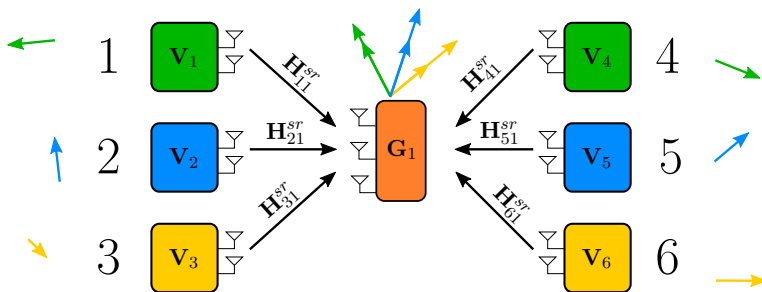


## Partially connected network

- ▶ Not all nodes are connected to all relays  $\Rightarrow$  Less interference
- ▶ Not all relays can help to perform IA in the whole network
- ▶ Requires local CSI

# IA in two-way relaying networks

## Concept of signal alignment



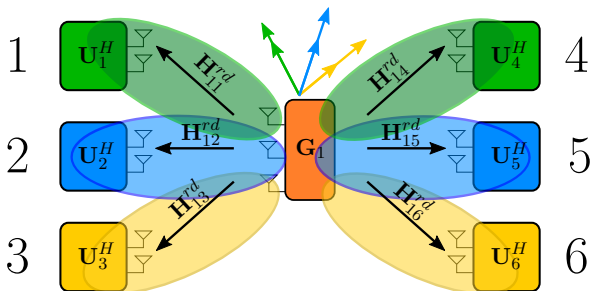
- ▶ **Signal alignment:** The communication partners transmit their signal to the relay such that the signals of each communication pair are aligned.

$$\text{span}(\mathbf{H}_{j1}^{sr} \mathbf{V}_j) = \text{span}(\mathbf{H}_{k1}^{sr} \mathbf{V}_k)$$

- ▶ **Assumption:** Self interference can be canceled

# IA in two-way relaying networks

## Concept of channel alignment

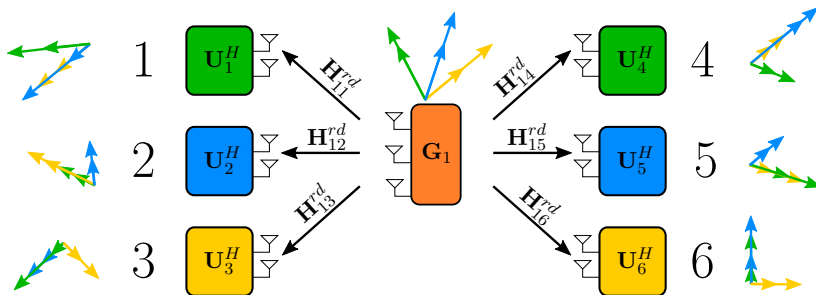


- **Channel alignment:** Each communication pair designs its receive filters such that the effective channels span the same subspace.

$$\text{span}(\mathbf{H}_{j1}^{rdH} \mathbf{U}_j) = \text{span}(\mathbf{H}_{k1}^{rdH} \mathbf{U}_k)$$

# IA in two-way relaying networks

## Transceive zero forcing

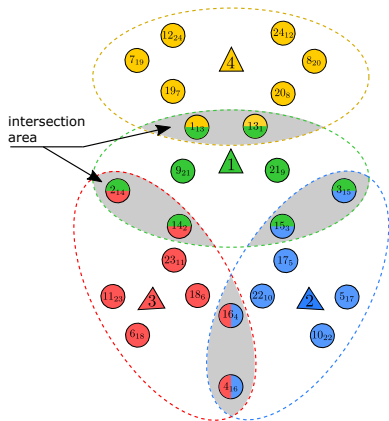


- ▶ **Transceive zero forcing:** The relay filter is designed such that all aligned links are orthogonal.

$$\mathbf{I} = \mathbf{H}_{\text{eff}q}^{\text{BC}} \cdot \mathbf{G}_q \cdot \mathbf{H}_{\text{eff}q}^{\text{MAC}}$$

# System model

## Partially connected network



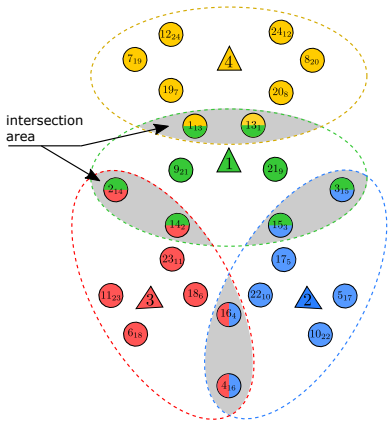
- ▶ Not all nodes are connected to all relays
- ▶ Some nodes are connected to multiple relays
- ▶ The network consists of partially connected subnetworks
  - ▶ Subnetwork = {Relay; connected node-pairs}
- ▶ Nodes inside the intersection area belong to more than one subnetwork

$j_k$  :  $j$  is the node-number and  $k$  its communication partner

$\triangle q$  :  $q$  is the relay-number

# Proposed algorithm

## One possible solution



- ▶ Most challenging part is the handling of the nodes inside the intersection area
- ▶ Each relay serves all connected node pairs
- ▶ Nodes inside an intersection area will be served by two relays
- ▶ Assumption: Only pairs of nodes are connected to a relay

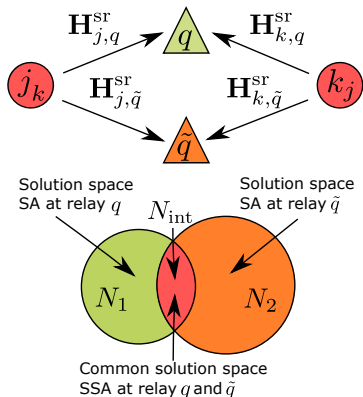
$j_k$  :  $j$  is the node-number and  $k$  its communication partner

$q$  :  $q$  is the relay-number



# Proposed algorithm

## Simultaneous Signal Alignment (SSA)

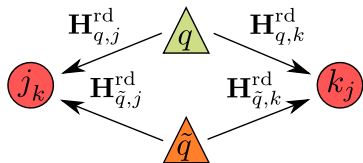


Performed in the multiple access (MAC) phase

- ▶ Signal alignment at relay  $q$ :  
 $\text{span}(\mathbf{H}_{j,q}^{sr} \mathbf{V}_{j,q}) = \text{span}(\mathbf{H}_{k,q}^{sr} \mathbf{V}_{k,q})$
- ▶ Results in solution space  $N_1$
- ▶ Signal alignment at relay  $\tilde{q}$ :  
 $\text{span}(\mathbf{H}_{j,\tilde{q}}^{sr} \mathbf{V}_{j,\tilde{q}}) = \text{span}(\mathbf{H}_{k,\tilde{q}}^{sr} \mathbf{V}_{k,\tilde{q}})$
- ▶ Results in solution space  $N_2$
- ▶ Solutions selected from  $N_{int}$  results in SSA at both relays simultaneously  
 $N_{int} = N_1 \cap N_2$
- ▶ Transmit spaces have to be large enough

# Proposed algorithm

## Simultaneous Channel Alignment (SCA)

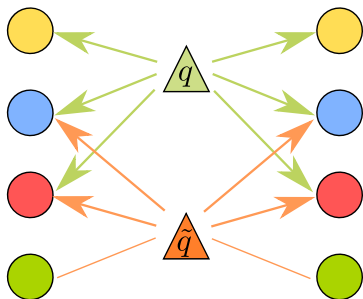


Performed in the broadcast (BC) phase

- ▶ Signal and channel alignment are dual problems
- ▶ Determination of the solution space is similar to determining the SA solution space.

# Proposed algorithm

## Transceive zero forcing (TRxZF)



- ▶ Receive zero forcing matrix

$$\mathbf{G}_q^{\text{RXH}} = (\mathbf{H}_{\text{eff}q}^{\text{MAC}})^{-1}$$

- ▶ Square matrix
- ▶ Non-singular

- ▶ Transmit zero forcing matrix

$$\mathbf{G}_q^{\text{TX}} = (\mathbf{H}_{\text{eff}q}^{\text{BC}})^{-1}$$

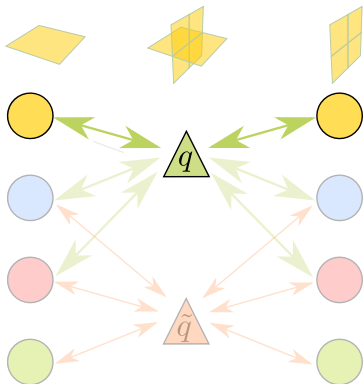
- ▶ Square matrix
- ▶ Non-singular

- ▶ Relay processing matrix

$$\mathbf{G}_q = \mathbf{G}_q^{\text{TX}} \cdot \mathbf{G}_q^{\text{RXH}} = (\mathbf{H}_{\text{eff}q}^{\text{MAC}} \cdot \mathbf{H}_{\text{eff}q}^{\text{BC}})^{-1}$$

# Proposed algorithm

## Counting the required dimensions of signal space (CDSS)



$d$ : Data streams

$|\mathcal{K}(q)|$ : Nodes connected to relay  $q$

$R_q$ : Antennas at each relay

$N_k$ : Antennas at each node

- ▶ Number of relay antennas:

- ▶ Number of effective data streams

$$R_q = \frac{1}{2} |\mathcal{K}(q)| d$$

- ▶ Number of antennas at each node:

- ▶ connected to relay  $q$ :

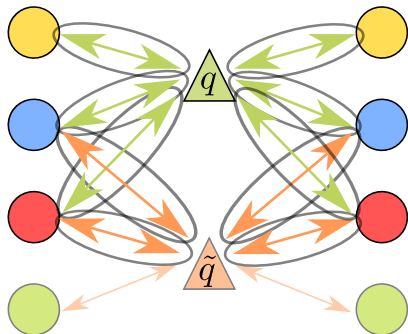
$$N_k \geq \frac{R_q + d}{2}$$

- ▶ connected to relay  $q$  and  $\tilde{q}$ :

$$N_k \geq \frac{R_q + R_{\tilde{q}} + d}{2}$$

- ▶ Large enough, such that a communication pair can select a common subspace at the common relay space

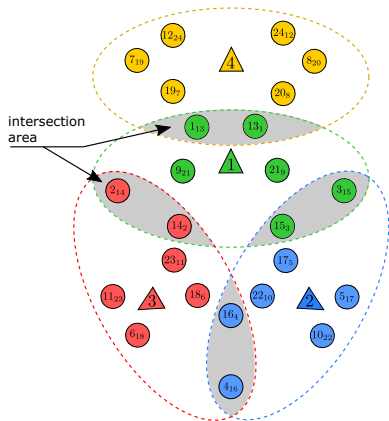
- ▶ Optimization is possible, if  $N_k$  is larger than the minimum required number



- ▶ Required CSI at the nodes:
  - ▶ Determined by SSA and SCA
  - ▶ Channels to all connected relays
  - ▶ **local CSI at the nodes**, to achieve IA
- ▶ Required CSI at the relays:
  - ▶ Determined by TRxZF
  - ▶ Effective channels of all nodes which are connected to a certain relay
  - ▶ **local CSI at the relays**, to achieve IA

# Simulation results

## Reference method



$j_k$ :  $j$  is the node-number and  $k$  its communication partner

$\triangle_q$ :  $q$  is the relay-number

### ► Proposed method

- Simultaneous signal and channel alignment in a partially connected network (SSCP\_closed)
- Nodes inside an intersection area will be served by several relay

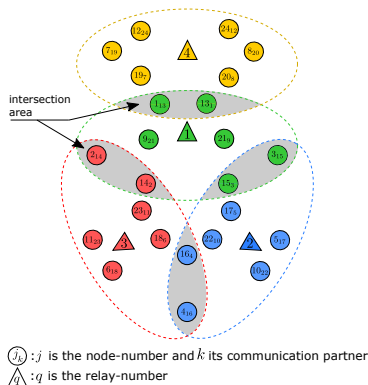
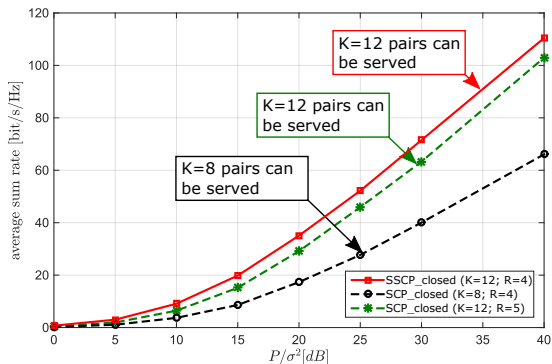
### ► Reference method

- Signal and channel alignment in a partially connected network (SCP\_closed)
- Nodes inside an intersection area will only be served by one relay
- The other relay treats these signals as interference and suppresses it

# Simulation results

Number of relays:  $Q = 4$ , Number of node antennas:  $N = 5$ ,

Number of data streams per node:  $d = 1$



- ▶ A partially connected network was introduced
- ▶ The new techniques called simultaneous signal and channel alignment were introduced to perform signal and channel alignment at multiple relays simultaneously
- ▶ Closed form solution was presented
  - ▶ Requires only local CSI
  - ▶ Requires less antennas at the relays than the reference method
  - ▶ Serves more communication pairs than the reference method
- ▶ Properness conditions was derived

# Thank you for your attention!