

Kombination adaptiver und nicht-adaptiver OFDMA-Übertragungsverfahren bei nicht perfekter Kanalkennntnis

Alexander Kühne, Anja Klein



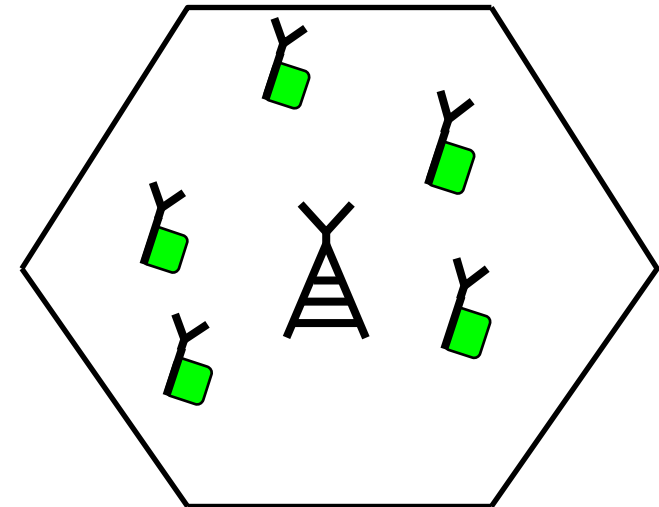
TECHNISCHE
UNIVERSITÄT
DARMSTADT

**Verbundprojekt:
Aufwandsgünstige Realisierung von hochperformanten OFDM-
Systemen mit partieller Kanalkennntnis**

Motivation



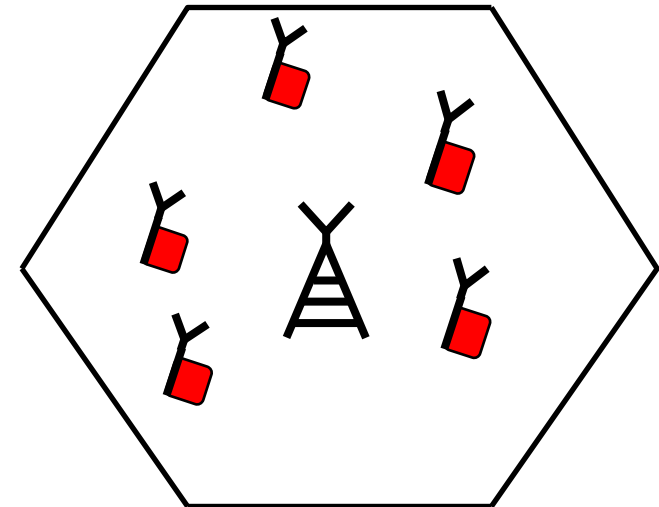
OFDMA	
Perfect CSIT <i>pure adaptive</i>	No CSIT <i>pure non-adaptive</i>



Motivation



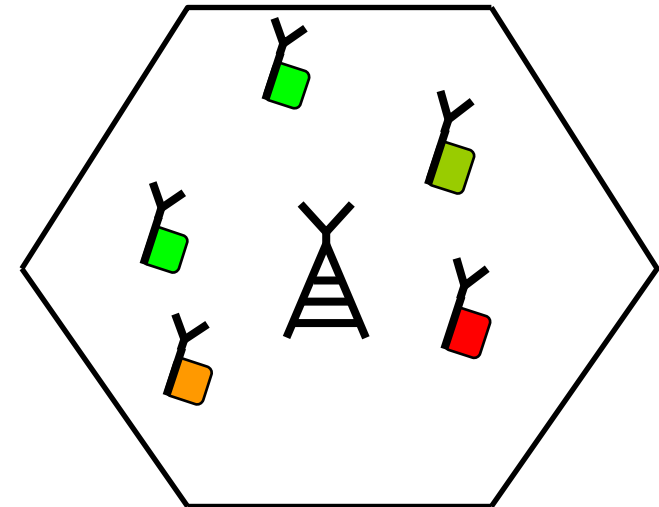
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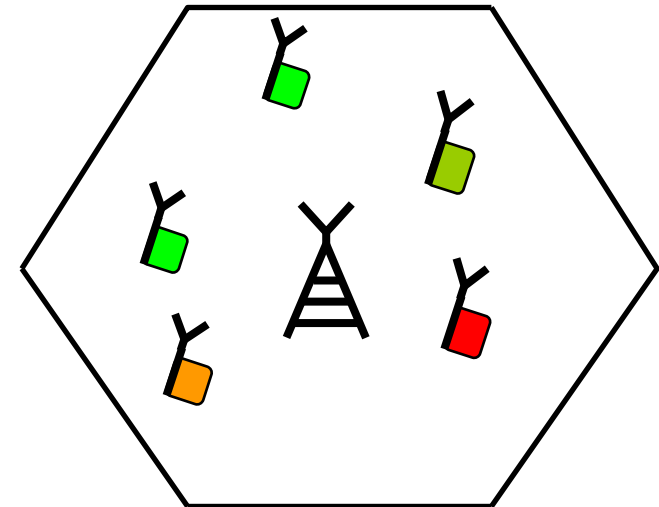
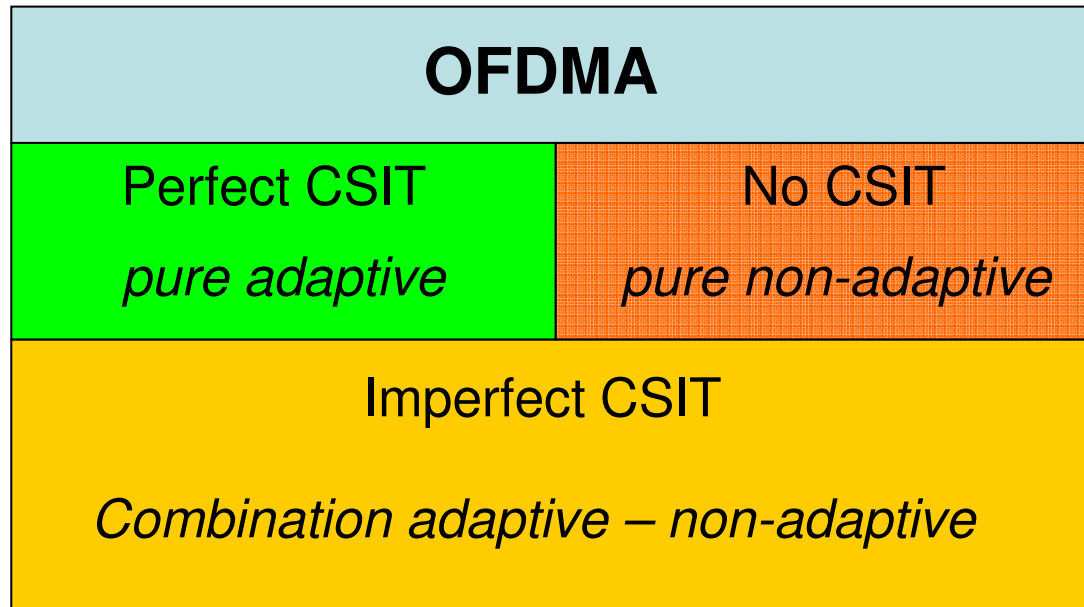
Motivation



OFDMA	
Perfect CSIT <i>pure adaptive</i>	No CSIT <i>pure non-adaptive</i>
Imperfect CSIT <i>Combination adaptive – non-adaptive</i>	



Motivation



How to combine adaptive and non-adaptive transmission ?

How to decide which user is served adaptively or non-adaptively ?

System model

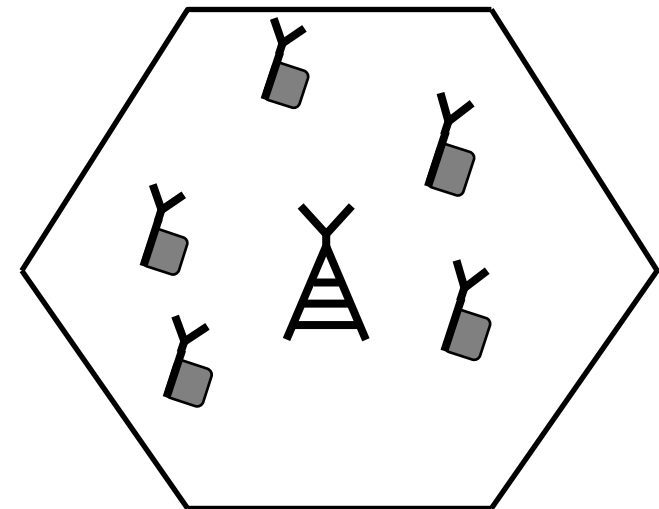
- OFDMA, N subcarriers
- Downlink
- One BS with one transmit antenna
- U MSs with one receive antenna each
- MSs uniformly distributed inside the cell
- Pathloss and i.i.d. Rayleigh fading
- Channel Quality Information (CQI): Instantaneous SNR of user u on subcarrier n in time slot k :

$$\gamma_u(n, k) = \bar{\gamma}_u \cdot |H_u(n, k)|^2$$

- CQI imperfect

- Outdated $\rho_u = J_0 \left(2\pi \cdot \frac{f_c}{c} \cdot v_u \cdot T \right)$

- Noisy estimates $\sigma_{E,u}^2 = (1 + \bar{\gamma}_u)^{-1}$

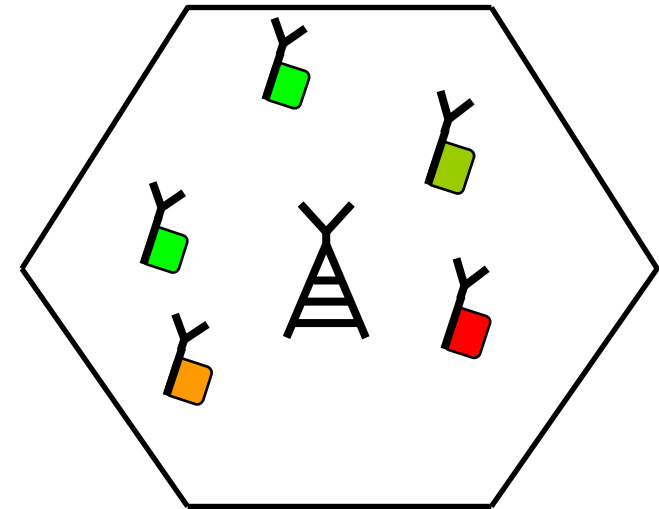


Combining adaptive and non-adaptive transmission



➤ Idea:

- Users with reliable CQI apply adaptive transmission
- Users with unreliable CQI apply non-adaptive transmission



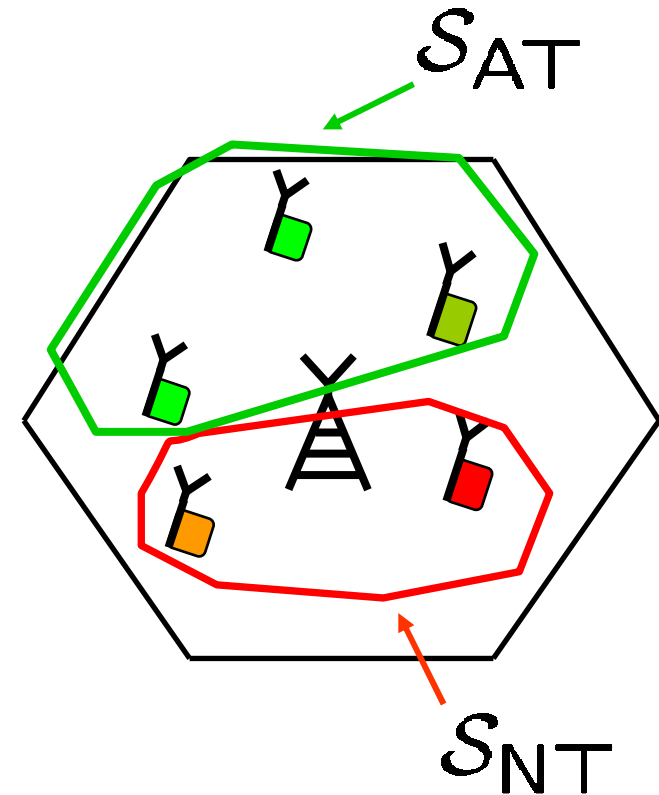
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➤ Divide users in two sets



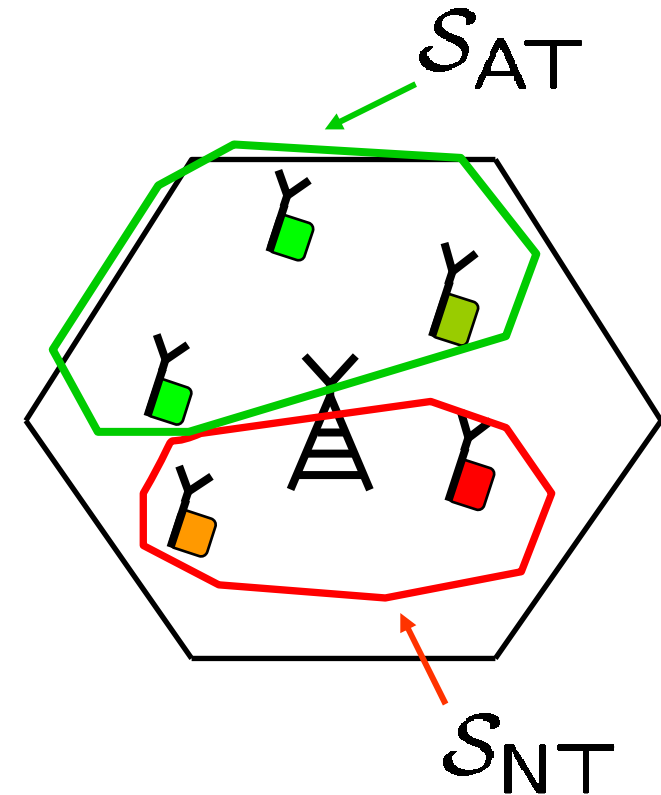
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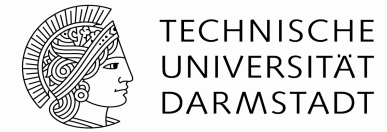
- Users with reliable CQI apply adaptive transmission
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➤ Divide users in two sets

- User data rate applying AT depends on number U_{AT} of adaptive users



Combining adaptive and non-adaptive transmission

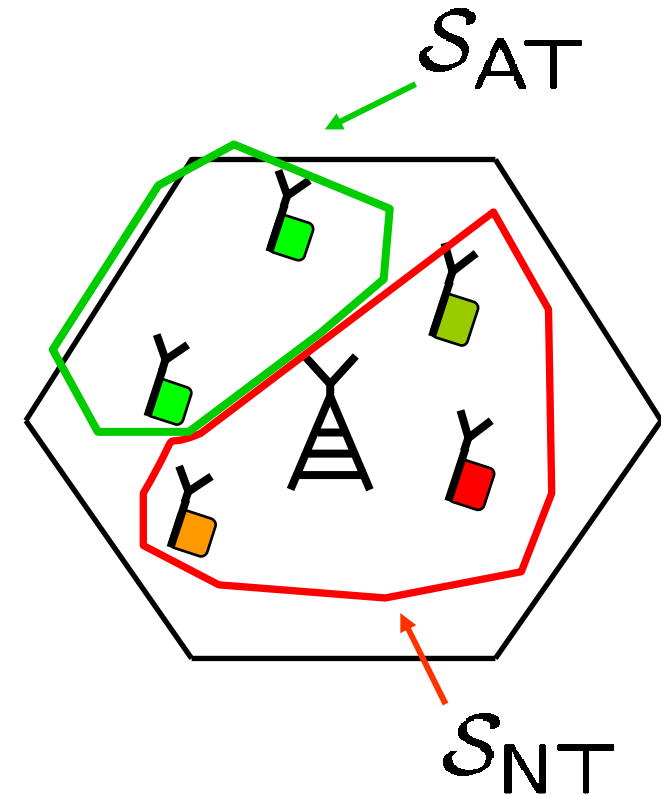


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➤ Divide users in two sets

- User data rate applying AT depends on number U_{AT} of adaptive users



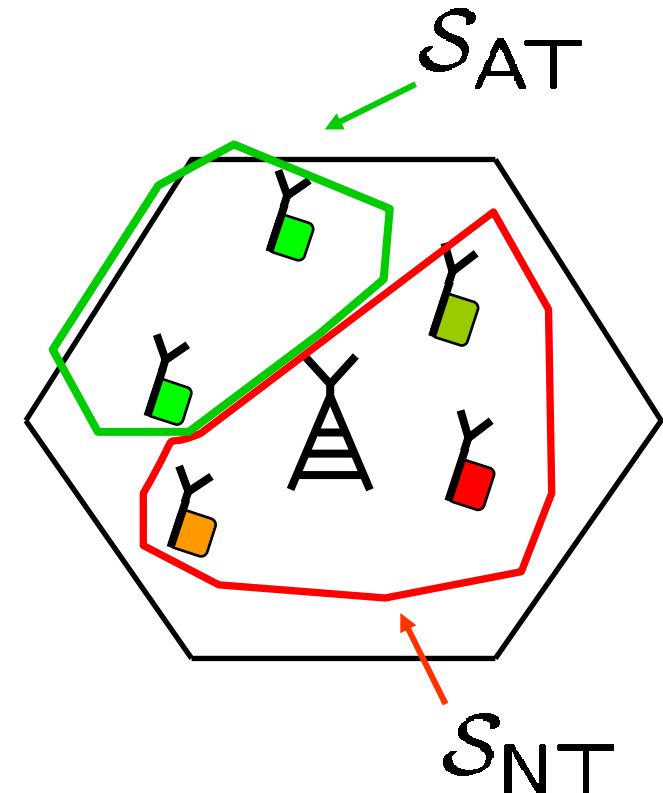
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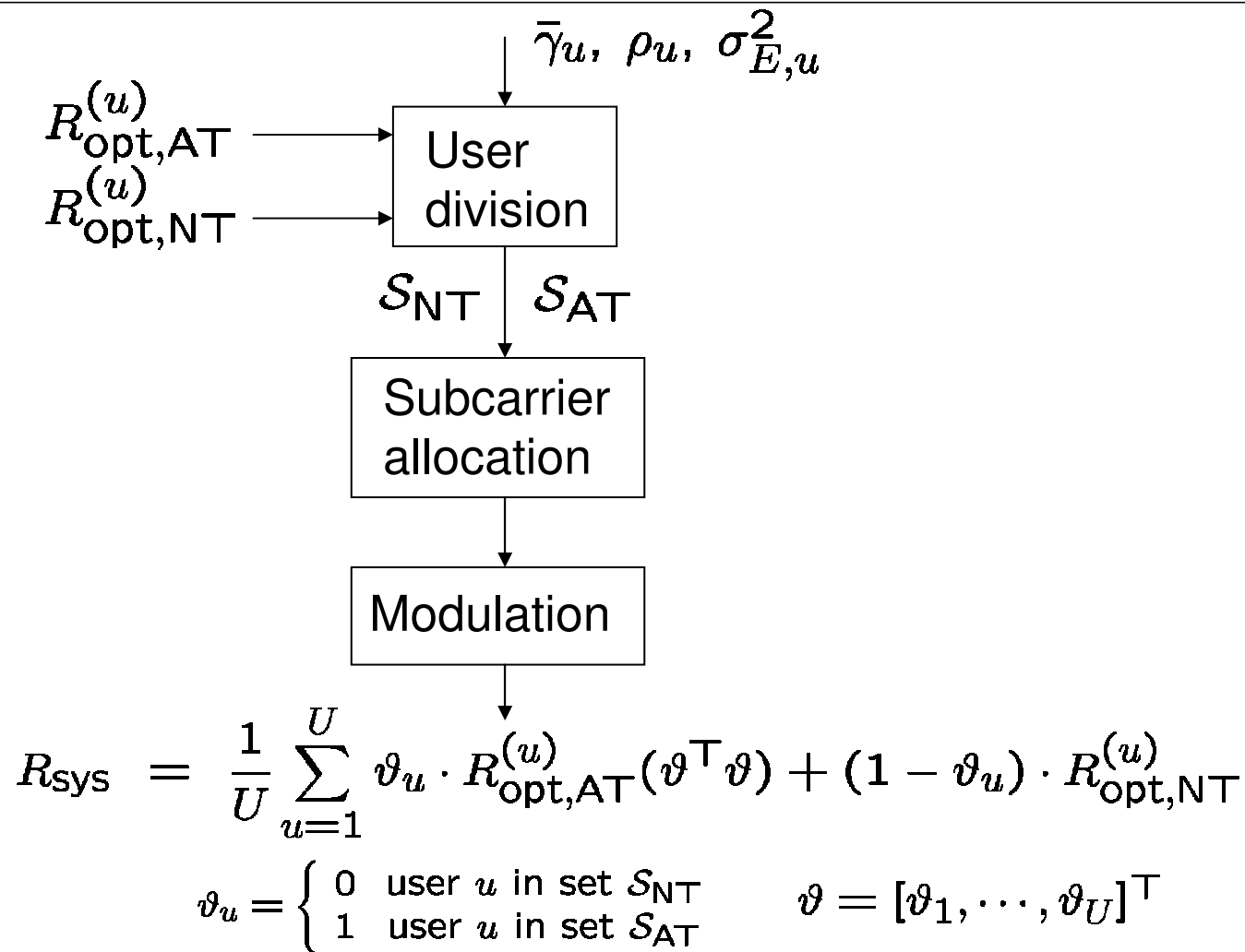
➤ Divide users in two sets

- User data rate applying AT depends on number U_{AT} of adaptive users
- Decision whether user u is an adaptive user or a non-adaptive user cannot be made user wise independent from the other users
- Joint consideration of all users

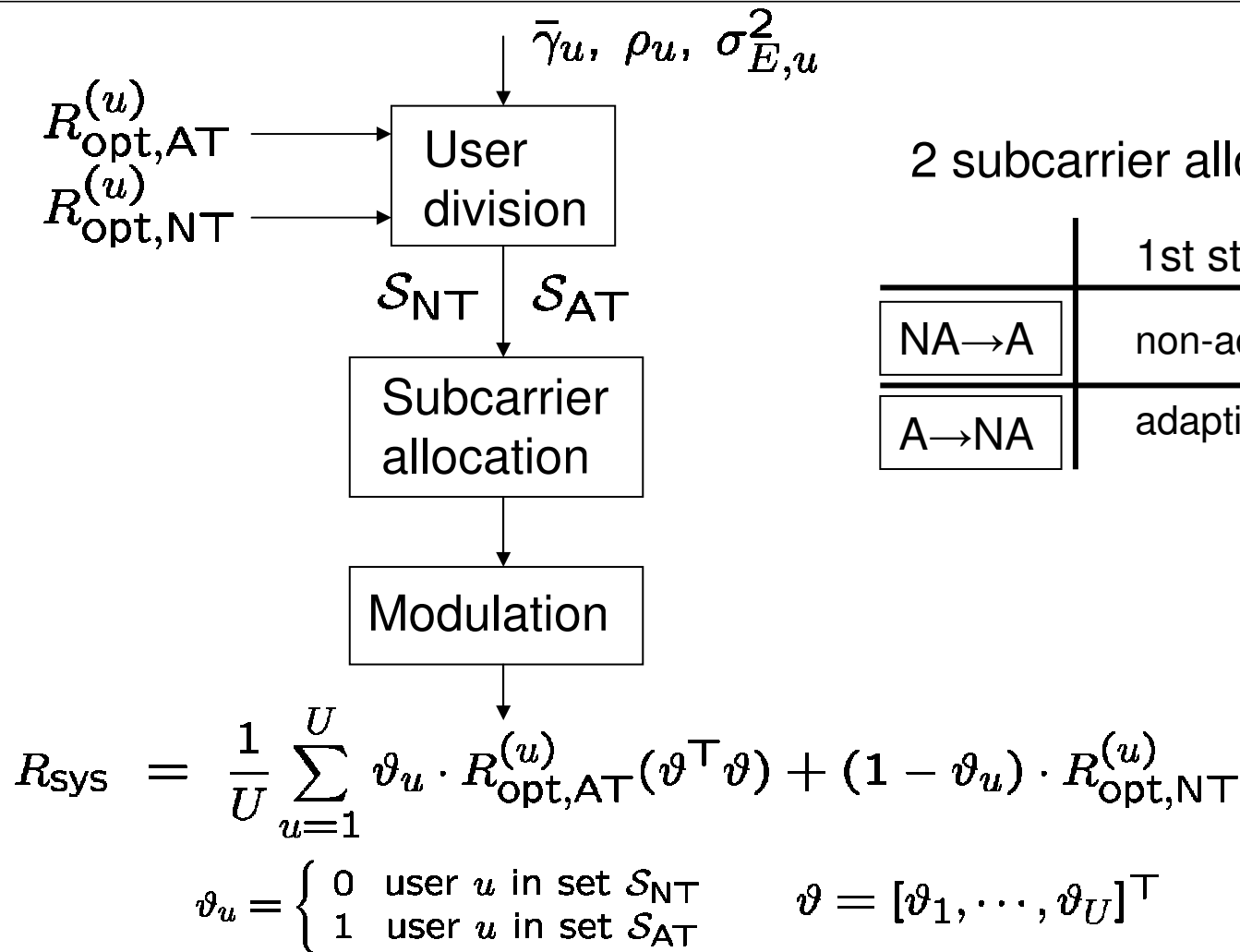




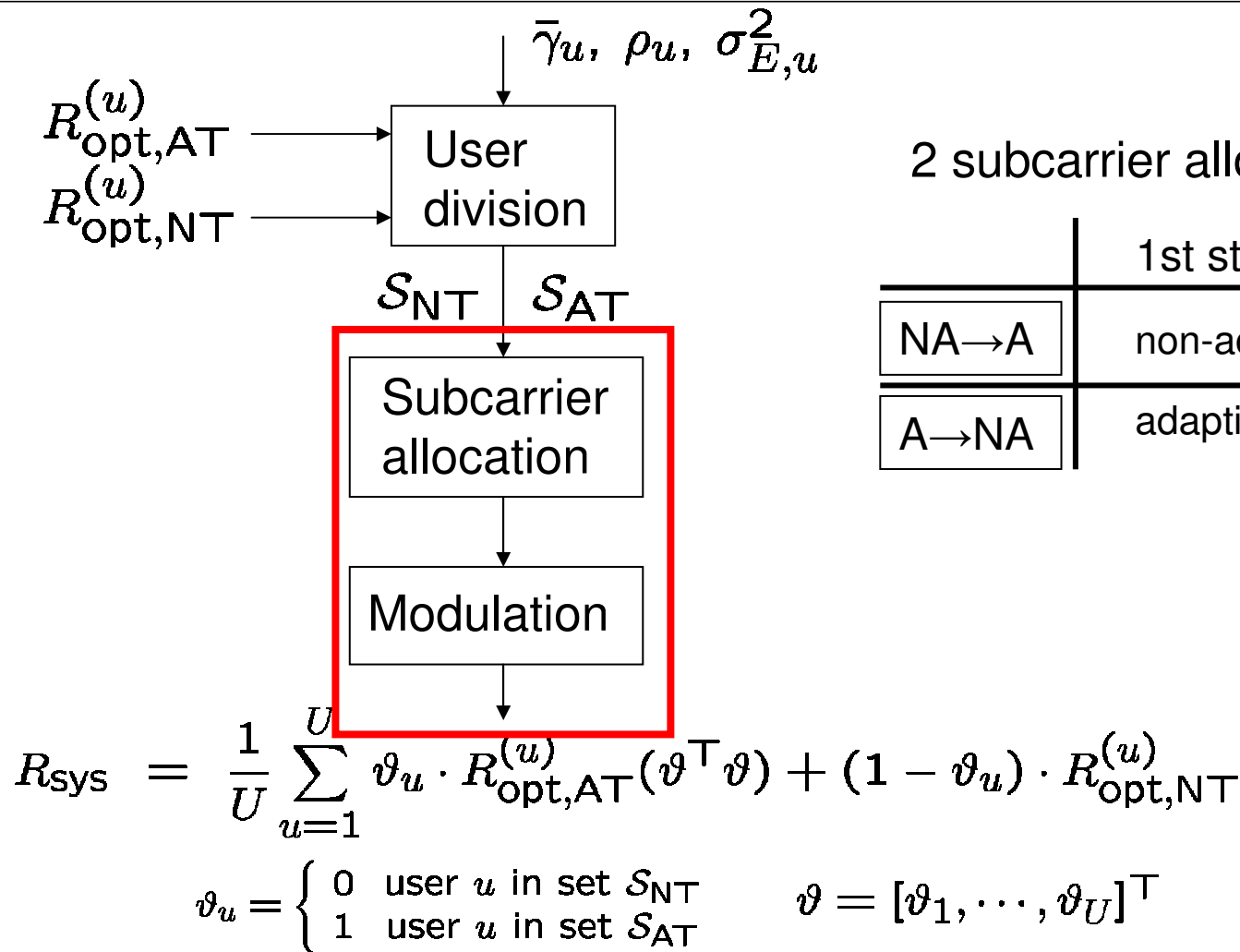
System overview



System overview



System overview



2 subcarrier allocation schemes:

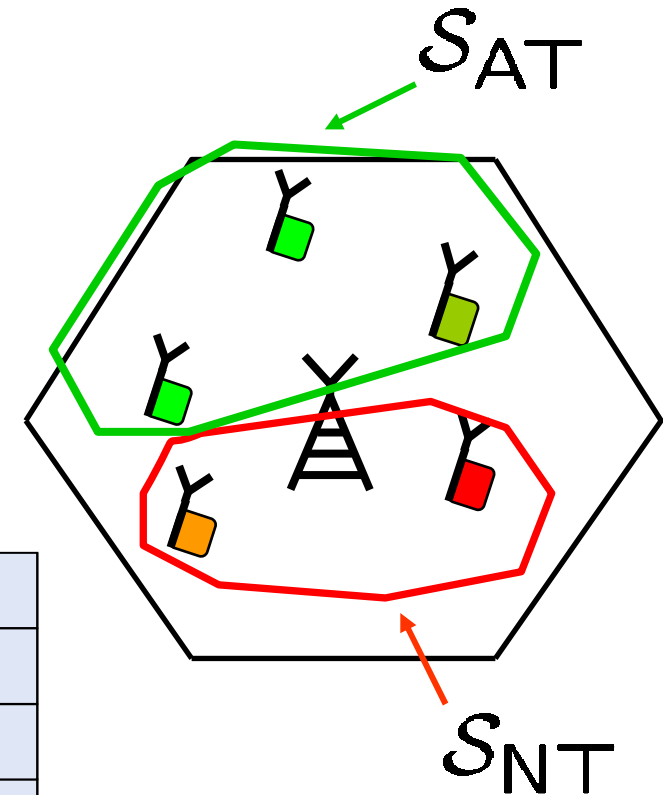
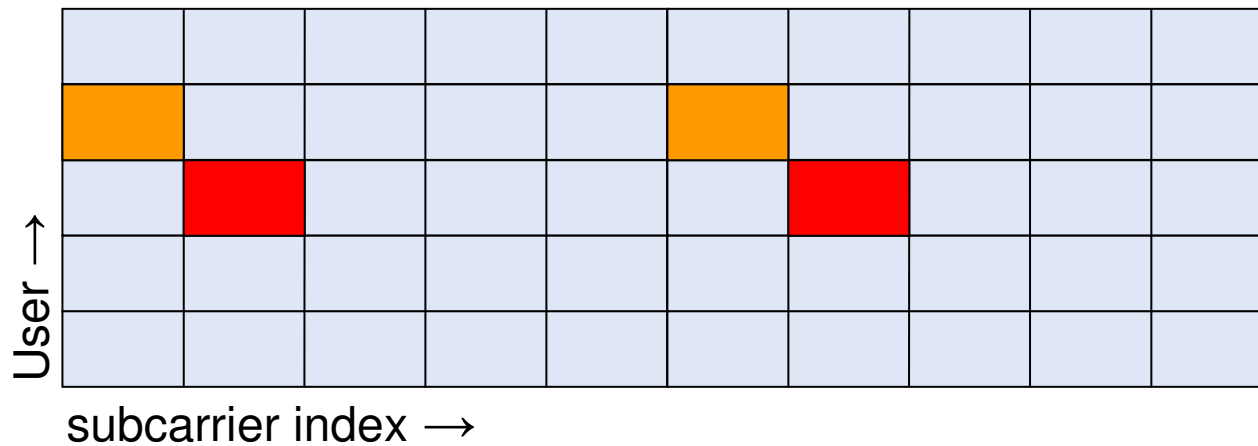
	1st step	2nd step
NA→A	non-adaptive	adaptive
A→NA	adaptive	non-adaptive

Subcarrier allocation

1) NA→A

- First allocate $N_U \cdot \text{card}\{S_{NT}\}$ subcarriers to users of set S_{NT}

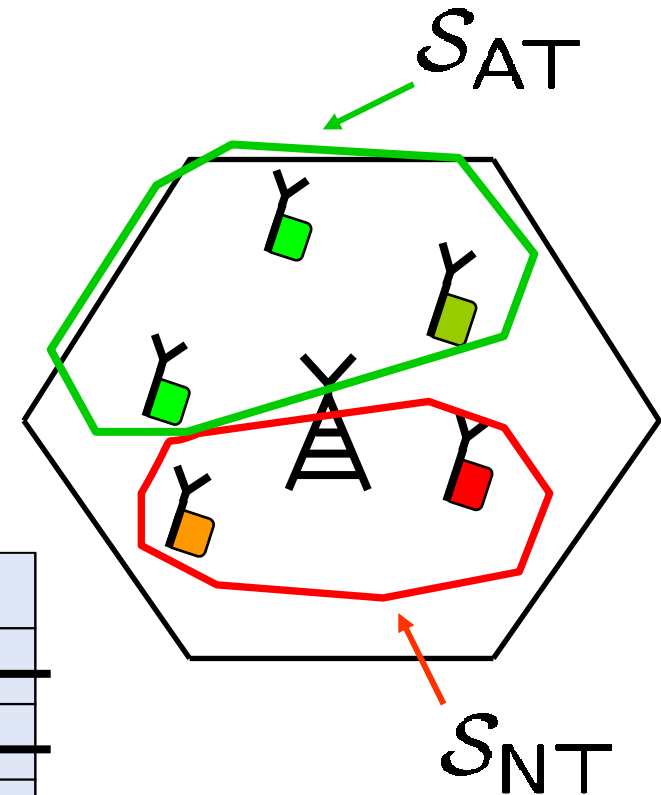
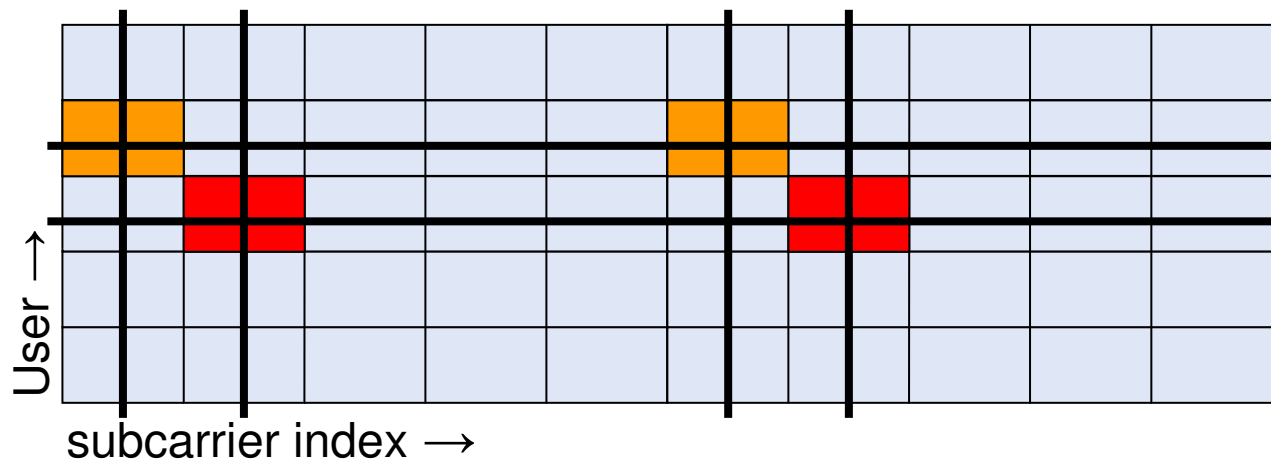
$$N_U = \frac{N}{U} \text{ Number of subcarriers per user}$$



Subcarrier allocation

1) $NA \rightarrow A$

- First allocate $N_U \cdot \text{card}\{S_{NT}\}$ subcarriers to users of set S_{NT}

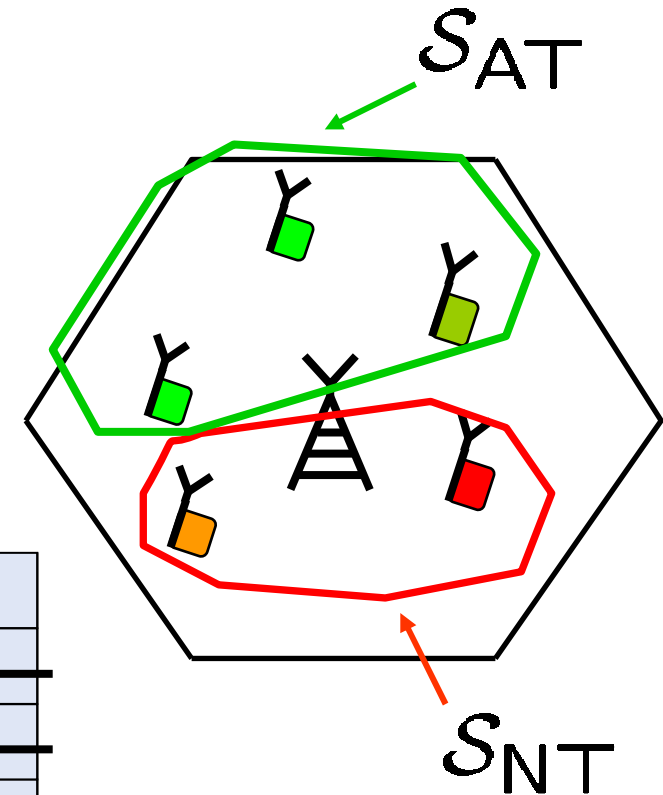
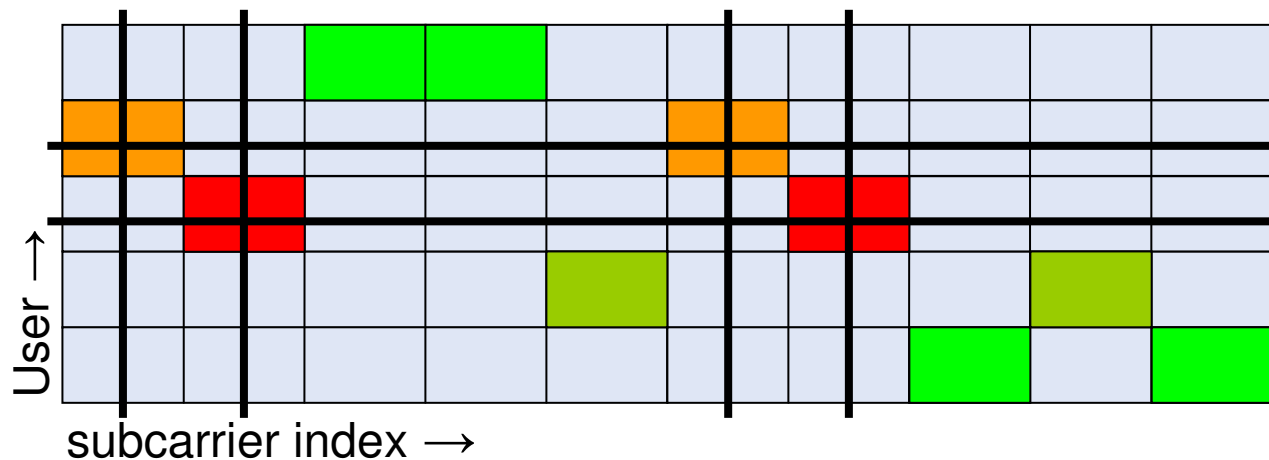


Subcarrier allocation

1) $NA \rightarrow A$

- First allocate $N_U \cdot \text{card}\{\mathcal{S}_{NT}\}$ subcarriers to users of set \mathcal{S}_{NT}
- Subsequently, allocate the remaining subcarriers to users of set \mathcal{S}_{AT} following Proportional Fair Scheduling approach

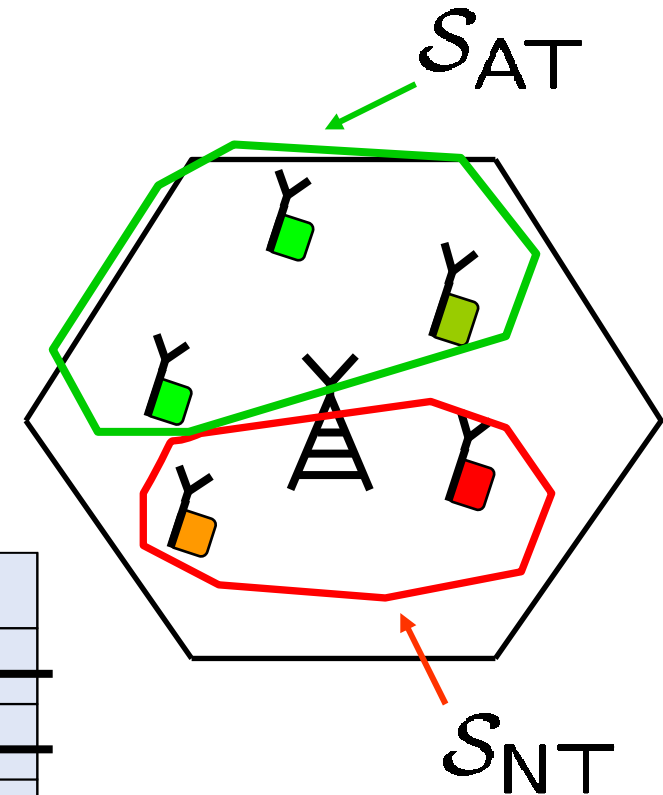
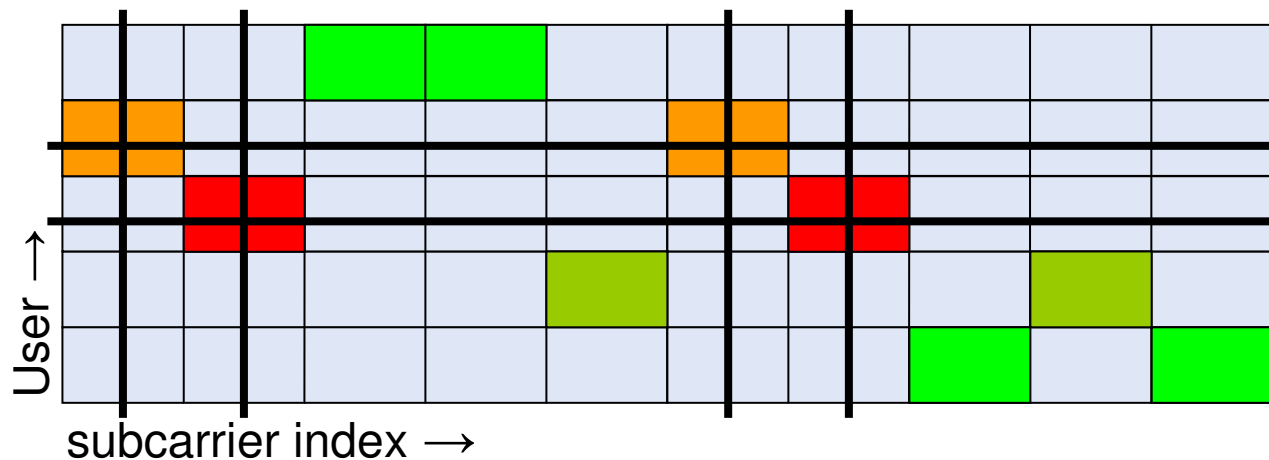
$$u^*(n, k) = \arg \max_u \left\{ \frac{\gamma_u(n, k)}{\bar{\gamma}_u} \right\}$$



Subcarrier allocation

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- First allocate $N_U \cdot \text{card}\{\mathcal{S}_{NT}\}$ subcarriers to users of set \mathcal{S}_{NT}
- Subsequently, allocate the remaining subcarriers to users of set \mathcal{S}_{AT} following Proportional Fair Scheduling approach
- Perform modulation (fixed and adaptive)



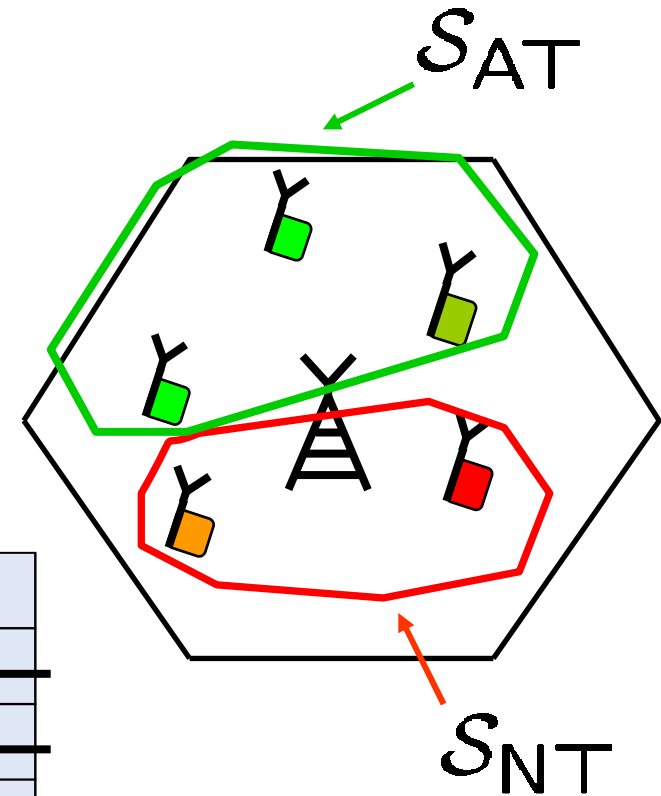
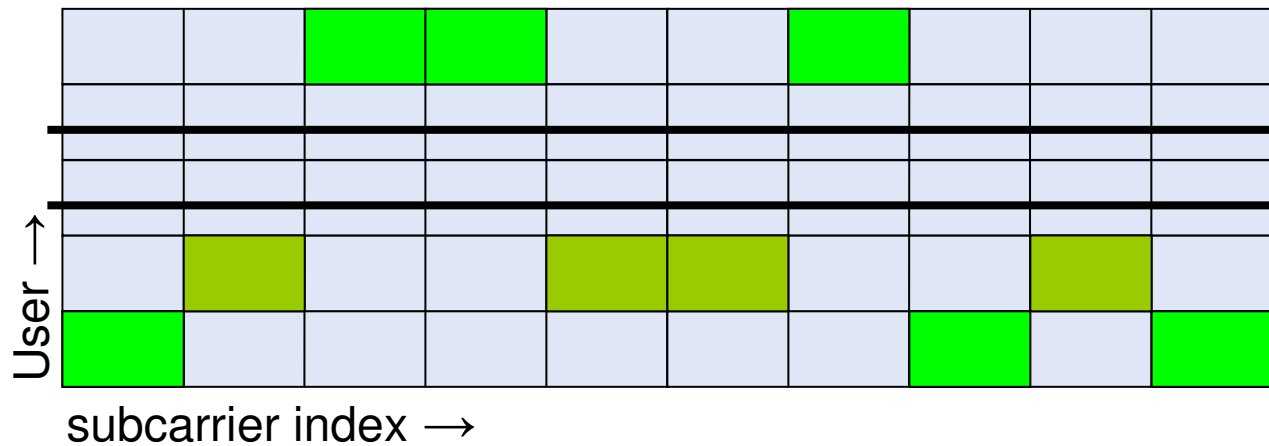
$$\gamma^{(u)} = [\gamma_0^{(u)}, \gamma_1^{(u)}, \dots, \gamma_M^{(u)}]^T$$

$$M = \text{card}\{\mathcal{M}\}$$

Subcarrier allocation

2) $A \rightarrow NA$

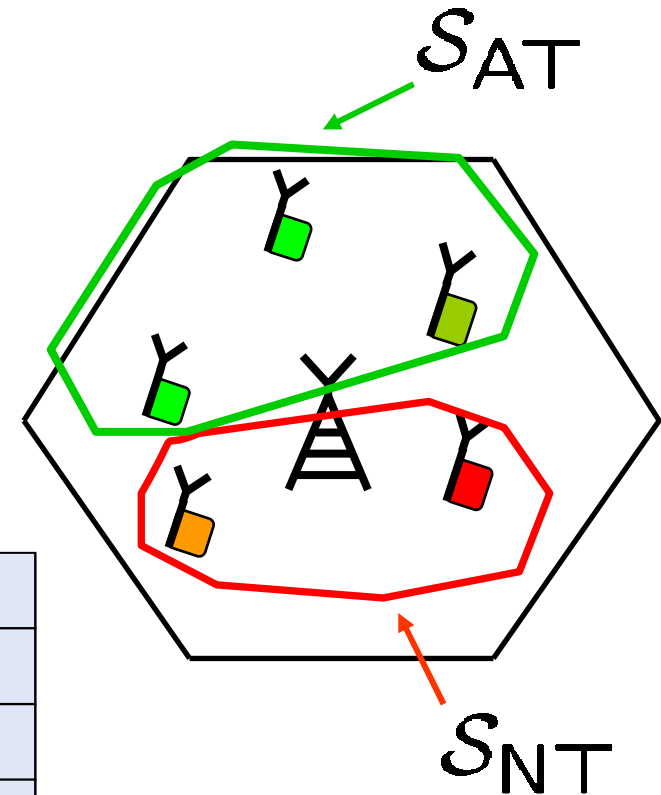
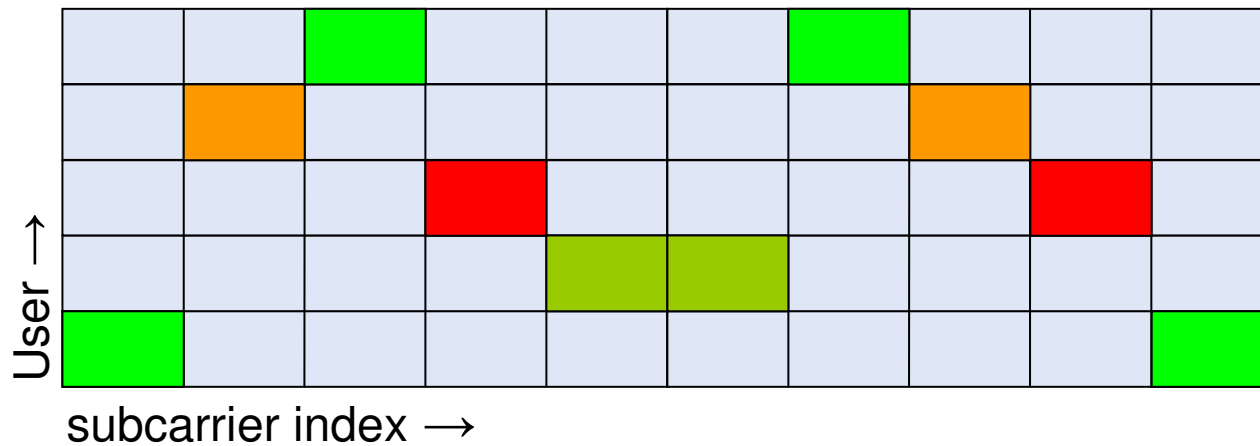
- First allocate all subcarriers to users of set S_{AT}



Subcarrier allocation

2) $A \rightarrow NA$

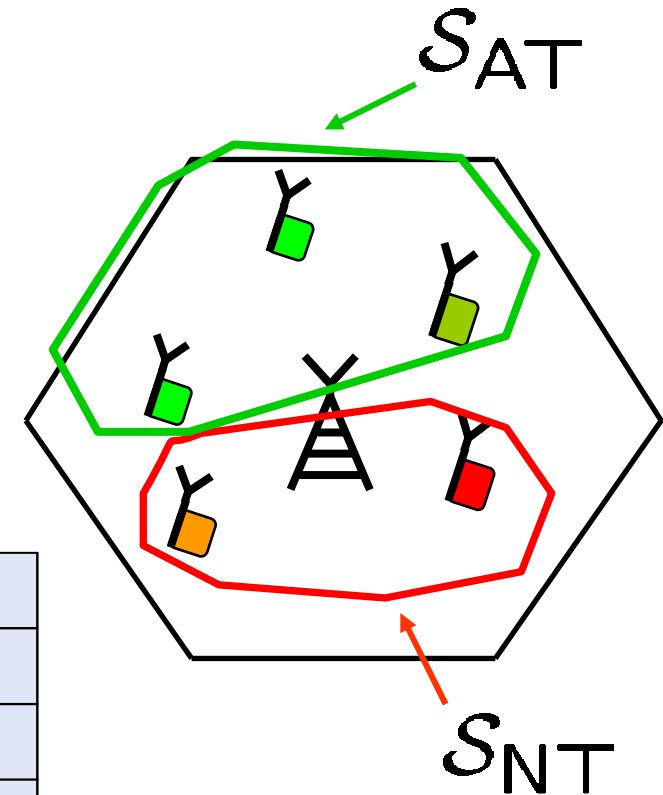
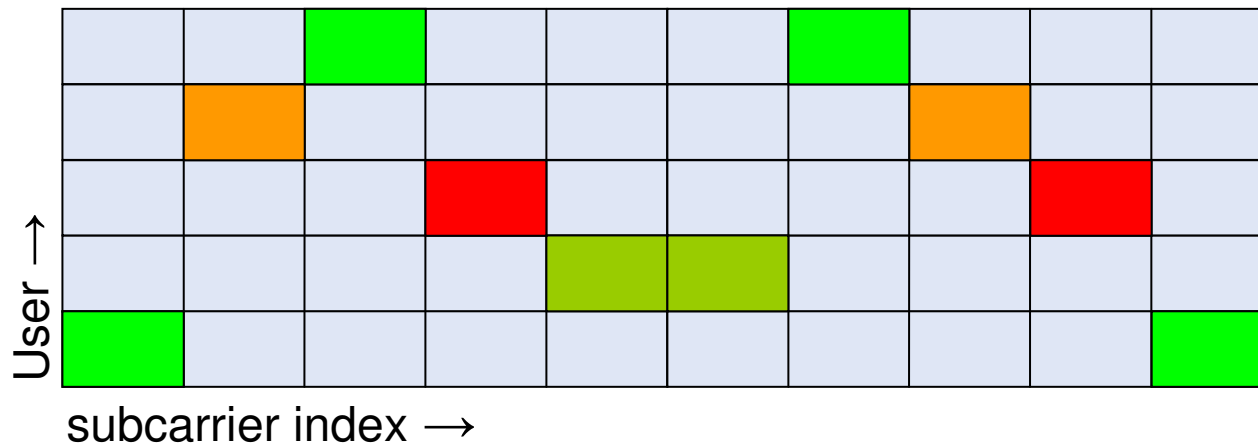
- First allocate all subcarriers to users of set \mathcal{S}_{AT}
- Select the $N_U \cdot \text{card}\{\mathcal{S}_{NT}\}$ worst subcarriers
- Re-allocate these subcarriers to users of set \mathcal{S}_{NT}



Subcarrier allocation

2) A → NA

- First allocate all subcarriers to users of set \mathcal{S}_{AT}
- Select the $N_U \cdot \text{card}\{\mathcal{S}_{NT}\}$ worst subcarriers
- Re-allocate these subcarriers to users of set \mathcal{S}_{NT}
- Perform modulation (fixed and adaptive)





Data rate and Bit Error Rate (BER)

Analytical expressions for the average user data rate and BER of user u taking into account imperfect CQI:

- User data rate for users in set \mathcal{S}_{AT} :

$$R_{AT}^{(u)} = f_i(\mathcal{M}, \bar{\gamma}_u, N_U, U_{AT}, \gamma^{(u)}, \sigma_{E,u}^2, \rho_u)$$

$$\overline{BER}_{AT}^{(u)} = f_i(\mathcal{M}, \bar{\gamma}_u, N_U, U_{AT}, \gamma^{(u)}, \sigma_{E,u}^2, \rho_u)$$

- User data rate for user in set \mathcal{S}_{NT} :

$$R_{NT}^{(u)} = f(\mathcal{M})$$

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i - Subcarrier allocation

$$i = \begin{cases} 1 & \text{NA} \rightarrow \text{A} \\ 2 & \text{A} \rightarrow \text{NA} \end{cases}$$

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$\bar{\gamma}_u$ - average SNR

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$\gamma^{(\mathbf{u})}$ - SNR thresholds

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$\sigma_{E,u}^2$ - Estimation error variance

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ρ_u - Correlation coefficient

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- Optimizing data rate:

$$R_{\text{opt},AT/NT}^{(u)} = \max \left(R_{AT/NT}^{(u)} \right)$$

subject to

$$\overline{BER}_{AT/NT}^{(u)} \leq BER_T$$

- User data rate for user in set \mathcal{S}_{NT} :

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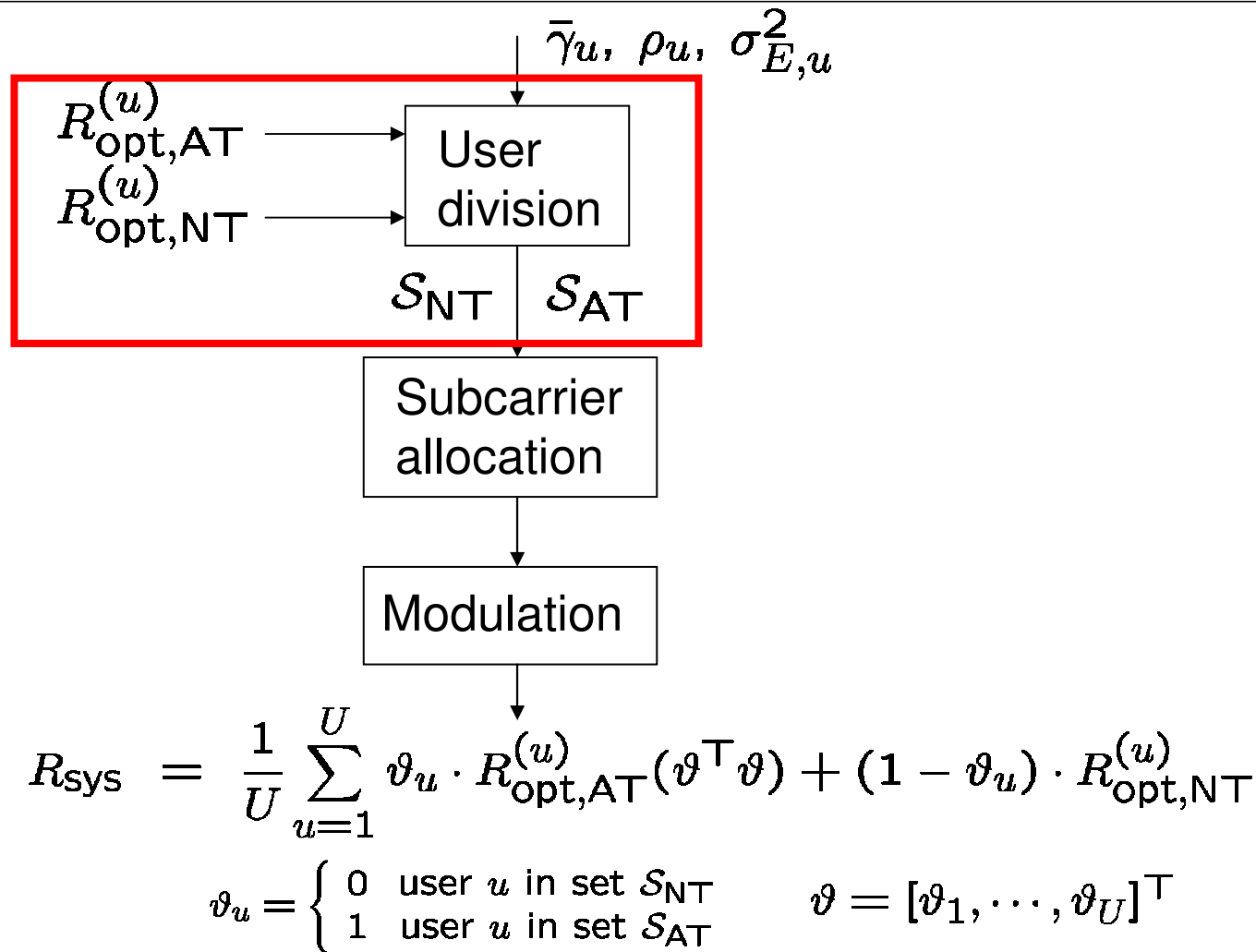


$$R_{opt,AT}^{(u)} = f_i(\bar{\gamma}_u, N_U, U_{AT}, \sigma_{E,u}^2, \rho_u)$$

$$R_{opt,NT}^{(u)} = f(\bar{\gamma}_u, N_U)$$



System overview



User division



- Aim: Maximize average system data rate, satisfy minimum user data rate

$$R_{\text{sys,opt}} = \max_{\vartheta} \left(\frac{1}{U} \sum_{u=1}^U \vartheta_u \cdot R_{\text{opt,AT}}^{(u)}(\vartheta^{\text{T}}\vartheta) + (1 - \vartheta_u) \cdot R_{\text{opt,NT}}^{(u)} \right)$$

subject to

$$R_{\text{opt}}^{(u)} \geq R_{\text{opt,NT}}^{(u)} \quad \forall u = 1, \dots, U$$

$$\vartheta = [\vartheta_1, \dots, \vartheta_U]^{\text{T}}$$



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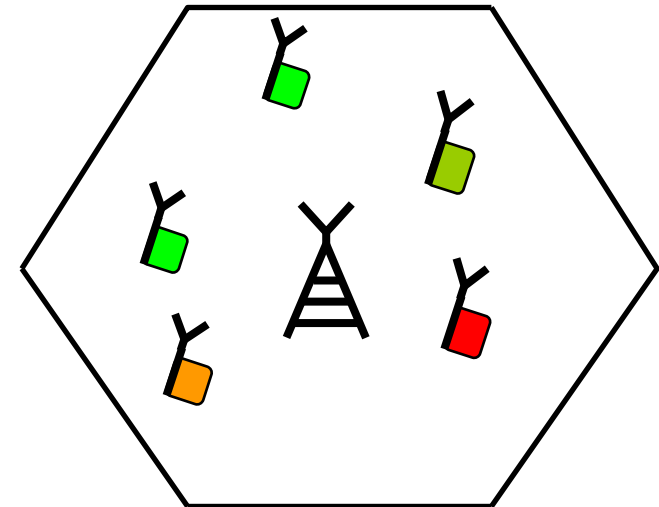
$$\vartheta = [\vartheta_1, \dots, \vartheta_U]^T$$

- Solutions and complexity:

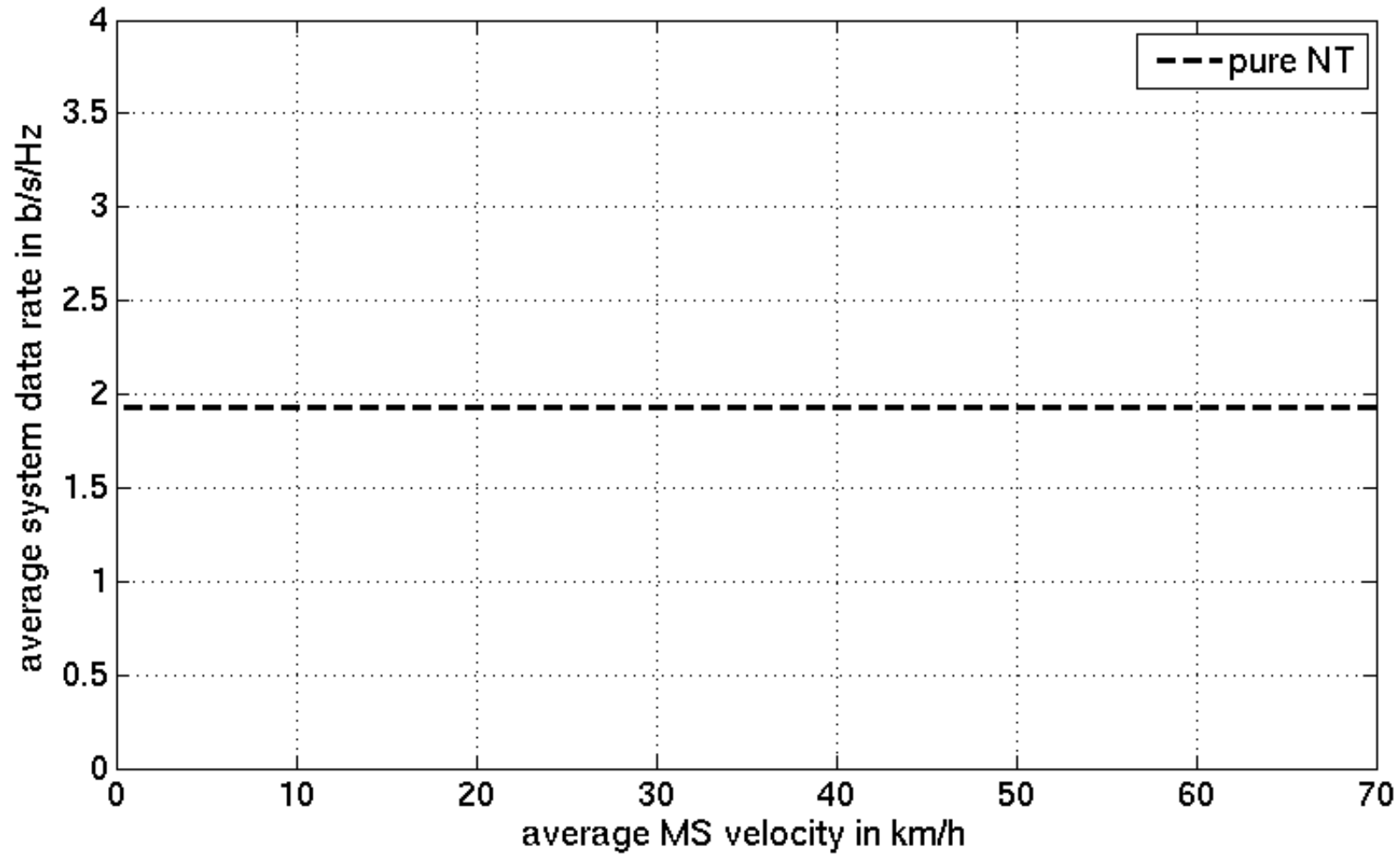
	NA→A	A→NA
Exhaustive Search	$\mathcal{O}(2^U)$	$\mathcal{O}(2^U)$
Set composition Number U_{AT} of users in set S_{AT} is important, not which users	$\mathcal{O}(U^3)$	$\mathcal{O}(U^3)$
Maximum number U_{AT} of users in set S_{AT} Determine maximum number U_{AT} which satisfies user data rate constraint	$\mathcal{O}(U^2)$	$\mathcal{O}(U^2)$ (suboptimal)

Numerical Results

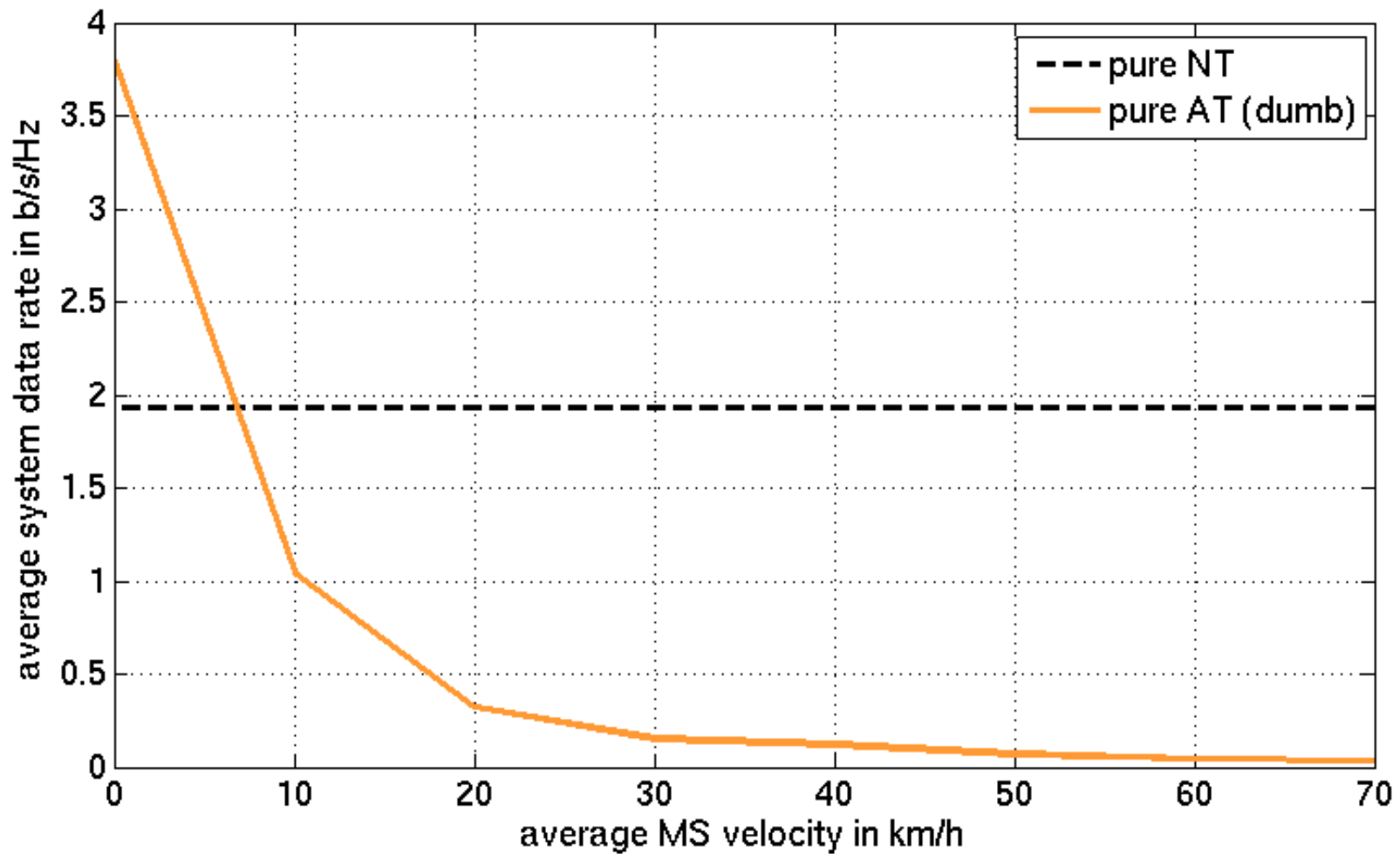
Number N of subcarriers	250
Number U of users	25
Cell radius R	300 m
Minimum distance d_0	10 m
Pathloss coefficient α	2.6
Modulation	uncoded M-PSK and M-QAM
Target bit error rate BER_T	$1 \cdot 10^{-3}$
Carrier frequency f_c	2 GHz
Time delay T	2 ms



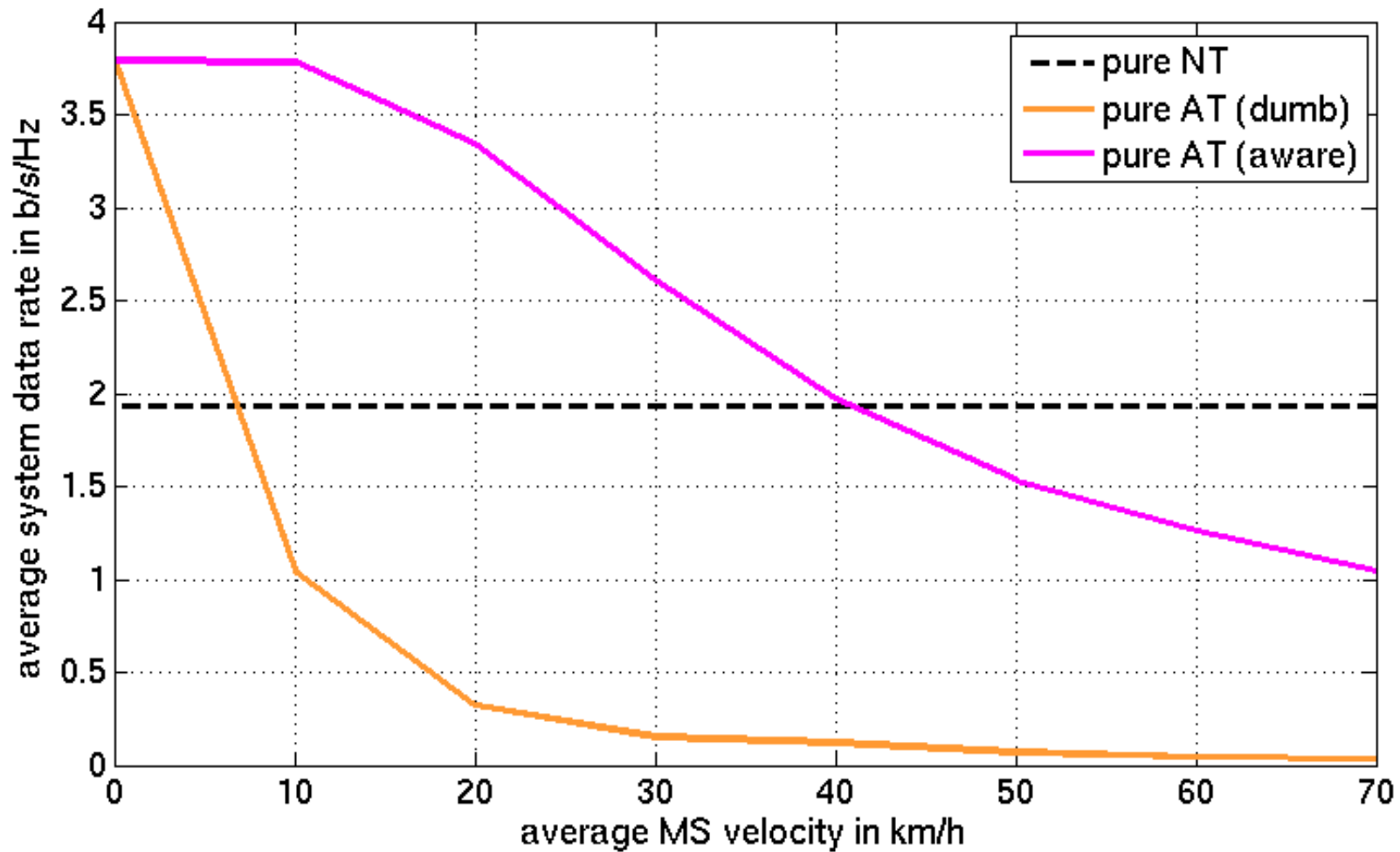
Results average system data rate **NA→A**



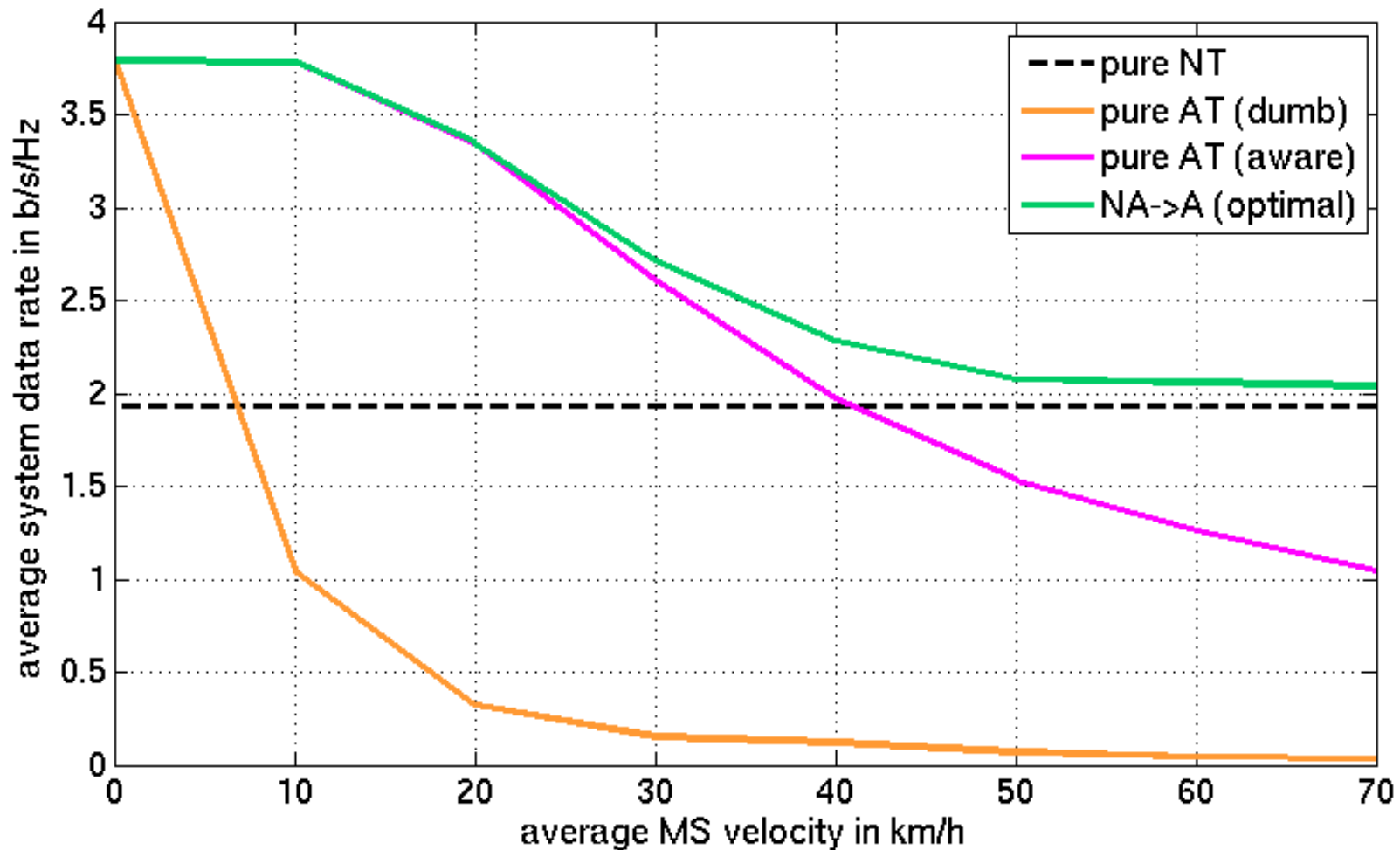
Results average system data rate NA→A



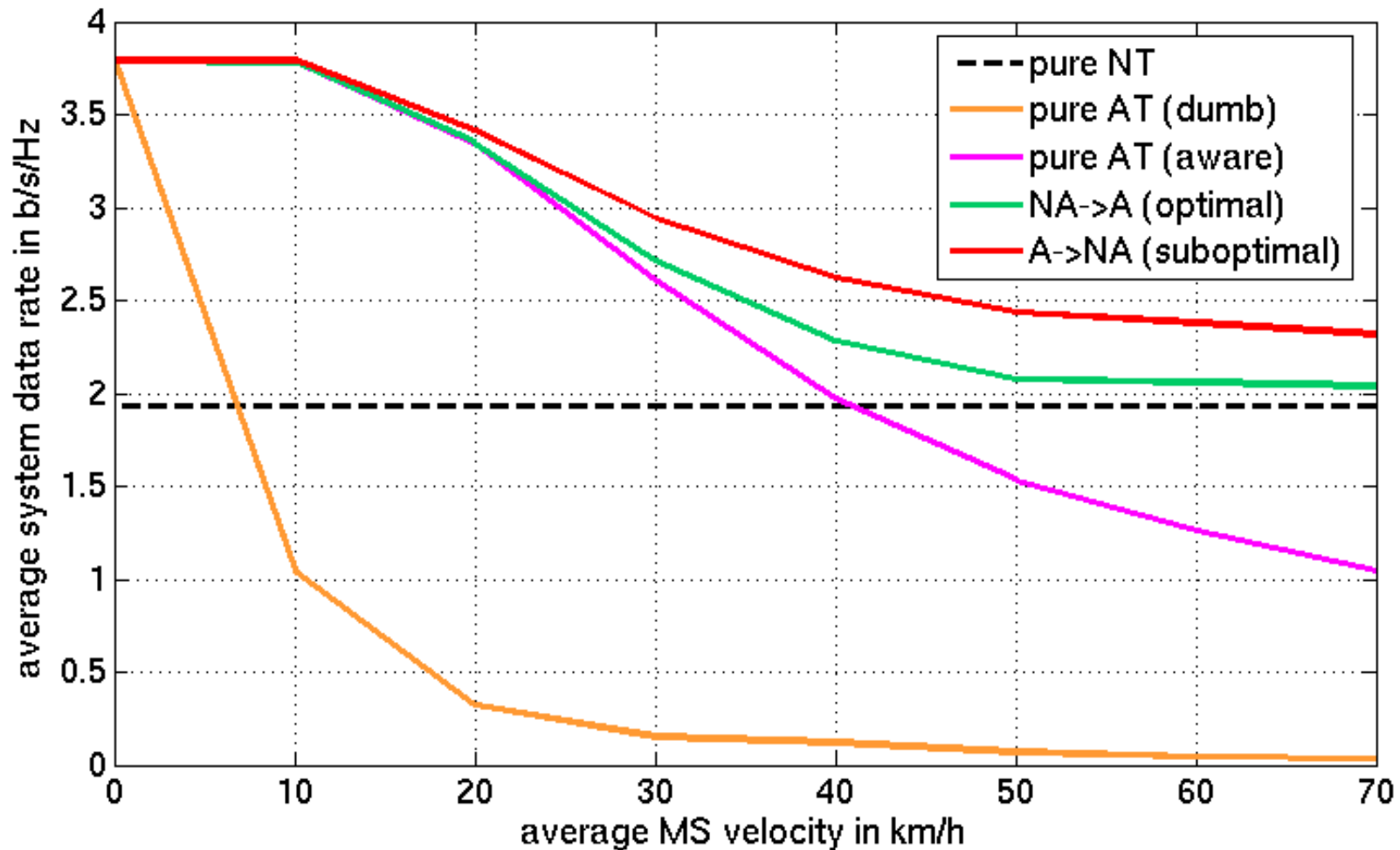
Results average system data rate **NA→A**



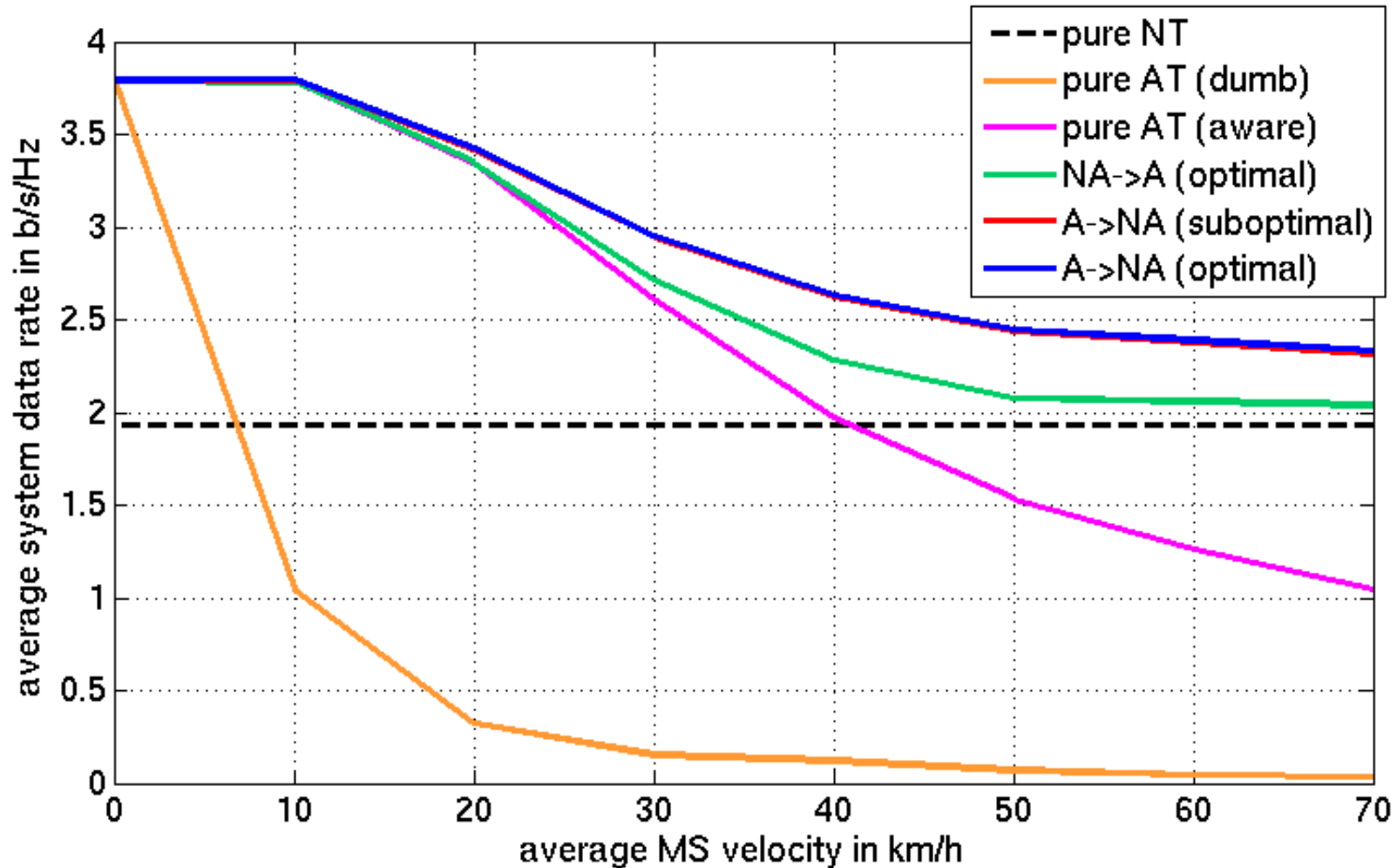
Results average system data rate NA→A



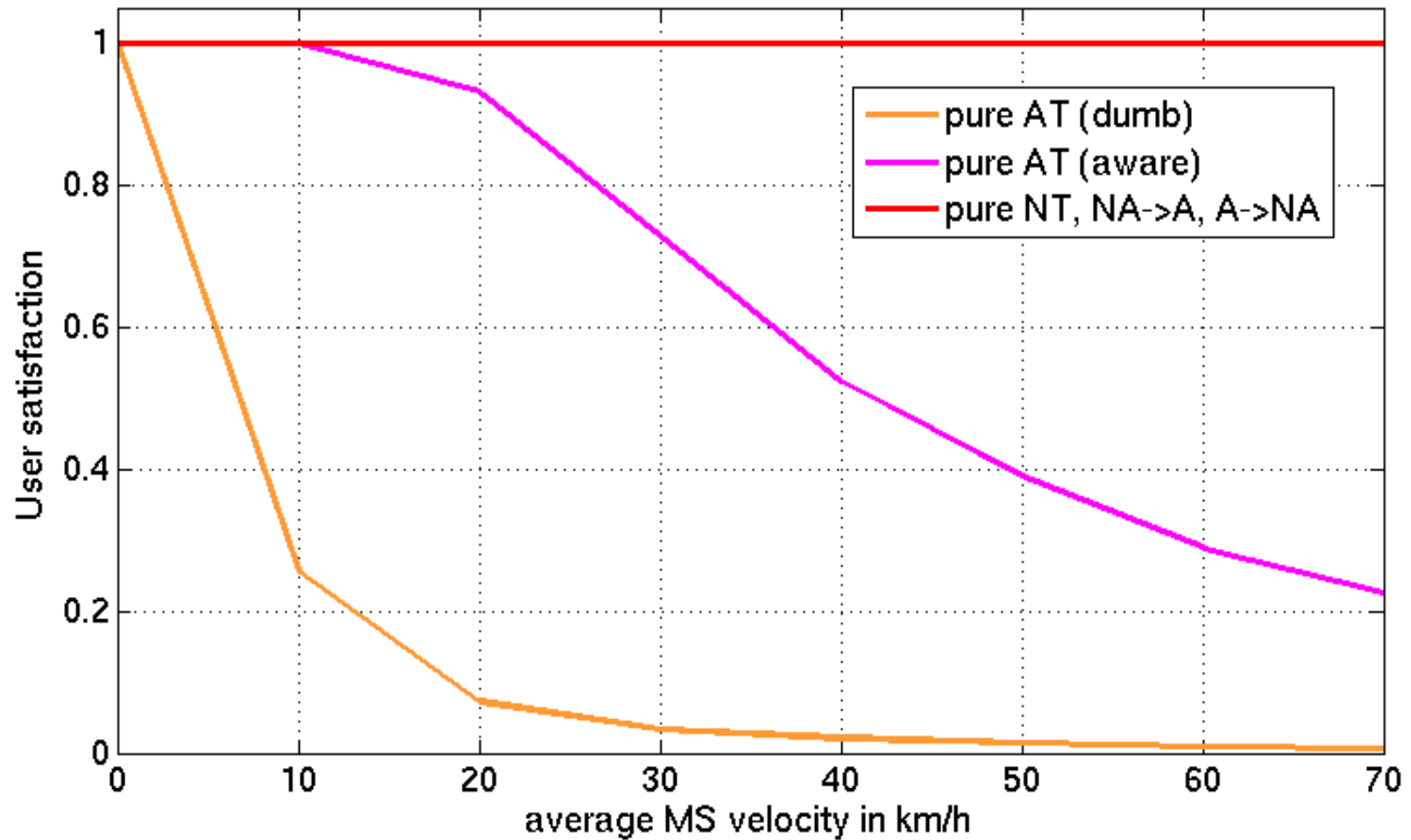
Results average system data rate $A \rightarrow NA$



Results average system data rate $A \rightarrow NA$



User satisfaction



Conclusions

- Combining of adaptive and non-adaptive multiuser OFDMA transmission schemes based on user division
- Two different subcarrier allocation schemes
- Two optimal and one suboptimal algorithm performing the user division based on analytical expressions for the user data rate and BER
- Both subcarrier allocation schemes outperform pure adaptive and pure non-adaptive subcarrier allocation schemes in the presence of imperfect CQI in terms of achievable data rate while satisfying minimum user data rate
- A→NA subcarrier allocation performs best

Publications



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Journal:

- A. Kühne and A. Klein, "Throughput analysis of Multi-user OFDMA-Systems using imperfect CQI feedback and diversity techniques," *IEEE Journal on Selected Areas in Communications*, vol. 26, no. 8, pp. 1440-1451, October 2008.

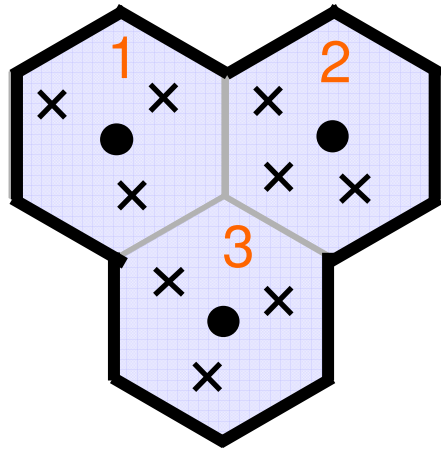
Conferences:

- A. Kühne and A. Klein, "An analytical consideration of imperfect CQI feedback on the performance of a multi-user OFDM-system," in *Proc. 12th International OFDM-Workshop*, Hamburg, Germany, August 2007.
- A. Kühne and A. Klein, "Adaptive subcarrier allocation with imperfect channel knowledge versus diversity techniques in a multi-user OFDM-system," in *Proc. International Symposium on Personal, Indoor and Mobile Radio Communications*, Athens, Greece, September 2007.
- A. Kühne and A. Klein, "Adaptive MIMO-OFDM using OSTBC with imperfect CQI feedback," in *Proc. International ITG Workshop on Smart Antennas*, Darmstadt, Germany, February 2008.
- A. Kühne and A. Klein, "Adaptive multiuser OFDMA systems with high priority users in the presence of imperfect CQI," in *Proc. 7th International Workshop on Multi-Carrier Systems & Solutions (MC-SS)*, Herrsching, Germany, May 2009 (to be published)

Joint contributions with project partner University of Rostock:

- A. Kühne, A. Klein, X. Wei and T. Weber, "Transmit Antenna Selection with imperfect CQI feedback in Multi-user OFDMA systems," in *Proc. 13th International OFDM-Workshop*, Hamburg, Germany, August 2008.
- X. Wei, T. Weber, A. Kühne and A. Klein, "Optimum MMSE Detection with Correlated Random Noise Variance in OFDM Systems," in *Proc. 13th International OFDM-Workshop*, Hamburg, Germany, August 2008.
- X. Wei, T. Weber, A. Kühne and A. Klein, "Joint Transmission with imperfect partial channel state information," in *Proc. IEEE Vehicular Technology Conference (VTC)*, Barcelona, Spain, April 2009 (to be published)

Joint transmission with imperfect partial CSI



- Multi-cell scenario
- Presentation Xinning Wei, University of Rostock, “Partial Channel-State Information in Cooperative Transmission”

